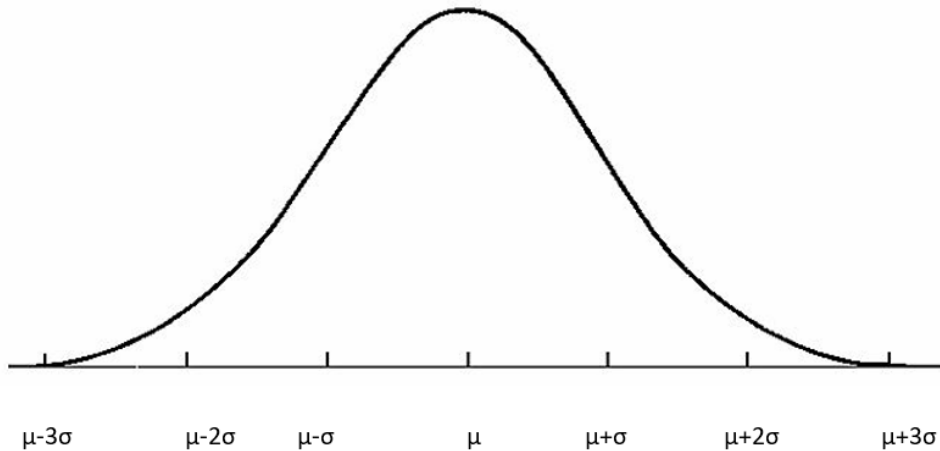


Statistics – TI84 Calculator

NORMAL DISTRIBUTION



Normalcdf: (2nd VARS (distr)) For a population that can be modelled by a Normal model centered at mean μ with standard deviation σ , $N(\mu, \sigma)$:

This function finds the percentage of the population (or probability) that

- 1) falls below a given value A : $normalcdf(-1EE99, A, \mu, \sigma)$
- 2) falls between two given values A and B : $normalcdf(A, B, \mu, \sigma)$
- 3) lies above a given value B : $normalcdf(B, 1EE99, \mu, \sigma)$

{ We use 1EE99 to represent $+\infty$ and -1EE99 to represent $-\infty$. EE is “2nd,” }

Example: Assuming a normal population has a mean of 24.8 and std dev of 6.2, $N(24.8, 6.2)$, what percentage of the population is less than 30.5?

$$normalcdf(-1EE99, 30.5, 24.8, 6.2) = .8210 \text{ or } 82.1\% \text{ of the population is less than } 30.5$$

invNorm (2nd VARS (distr)) For a population that can be modelled by a Normal model centered at mean μ with standard deviation σ , $N(\mu, \sigma)$:

This function finds the n th percentile. That is, the value that has $n\%$ of the population below it.

$$nth \text{ percentile value} = invNorm(n, \mu, \sigma)$$

Example: Assuming a normal population has a mean of 24.8 and std dev of 6.2, $N(24.8, 6.2)$, what is the 40th percentile (40% of the population is below what value)?

$$invNorm(.4, 24.8, 6.2) = 23.229 \text{ or } 40\% \text{ of the population is below } 23.229$$

z-score is a standardized value. It represents how many standard deviations above (or below) a data value is from the mean. Z-scores have a mean of 0 and a standard deviation of 1.

$$z = \frac{y - \mu}{\sigma}$$

Normalcdf and invNorm can be used with z-scores

To find the percentage of the population that falls:

- 1) below a given value: Find the z-score for the value. Then calculate $normalcdf(-1e99, z, 0, 1)$
- 2) falls between 2 values: Find the z-score for each value. Then calculate $(z_1, z_2, 0, 1)$
- 3) lies above a given value: Find the z-score for the value. Then calculate $normalcdf(z, 1e99, 0, 1)$

{The calculator default is mean 0 and std dev 1}

Example: Assuming a normal population has a mean of 24.8 and std dev of 6.2, $N(24.8, 6.2)$, what percentage of the population is less than 30.5?

$$z = \frac{30.5 - 24.8}{6.2} = .919355$$

$$normalcdf(-1e99, .919355) = .8210 \text{ or } 82.1\% \text{ of the population is less than } 30.5$$

{keep many decimals in z-score calculation or the normalcdf calculation will be “off”}

To find the nth percentile z-score:

First find the nth percentile z-score = $invNorm(n, 0, 1)$

Next use z-score formula to solve for the nth percentile value

Example: Assuming a normal population has a mean of 24.8 and std dev of 6.2, $N(24.8, 6.2)$, what is the 40th percentile (40% of the population is below what data value?)?

$$invNorm(.4, 0, 1) = -.253347 = 40^{th} \text{ percentile z-score}$$

$$z = -.253347 = \frac{y - 24.8}{6.2}$$

solve for y

$$y = 23.229 \text{ 40\% of the population is below } 23.229$$

{keep many decimals in invNorm output or the y calculation will be “off”}